

19A**Acids and Bases**

Extra Practice Problems

Calculating pH

Common logarithms have the property that the log of ten raised to some power is equal to the exponent. For example, the logarithm of 10^2 is two; $\log 10^2 = 2$. The logarithm of 10^{-5} is minus five; $\log 10^{-5} = -5$. The pH scale is based upon logarithms, and it is a convenient way to express the hydrogen ion concentration of a solution. It is defined as follows: $\text{pH} = -\log [\text{H}^+]$. The ion-product constant for water, K_w , relates the concentrations of hydrogen ion and hydroxide ion in water or in an aqueous solution.

$$K_w = [\text{H}^+] \times [\text{OH}^-] = 1.0 \times 10^{-14} (\text{mol/L})^2$$

Taking the negative logarithm of each term in the expression for K_w gives the following.

$$\begin{aligned}\log[\text{H}^+] + -\log[\text{OH}^-] &= -\log(1.0 \times 10^{-14}) \\ \text{pH} + \text{pOH} &= 14.00\end{aligned}$$

A solution is neutral when $\text{pH} = \text{pOH} = 7.0$. An acidic solution has a $\text{pH} < 7.0$ and a $\text{pOH} > 7.0$. A solution that is basic has a $\text{pH} > 7.0$ and a $\text{pOH} < 7.0$.

Example A

A solution has a hydrogen ion concentration of $1 \times 10^{-6}M$. What is its pH?

Solution

$$\begin{aligned}\text{pH} &= -\log[\text{H}^+] \\ \text{pH} &= -\log(1 \times 10^{-6}) \text{ \{reminder: the } \log(a \times b) = \log a + \log b\} \\ \text{pH} &= -(0.0 + (-6)) \text{ \{reminder: the } \log 1 = 0.0\} \\ \text{pH} &= +6.0\end{aligned}$$

19.4

You Try It

1. What is the pH of a solution with $[\text{H}^+] = 1 \times 10^{-3}M$?

Your Solution

19.4

Example B

What is the pH of a solution if the $[\text{H}^+] = 7.2 \times 10^{-9}M$?

Solution

$$\begin{aligned}\text{pH} &= -\log[\text{H}^+] \\ &= -\log(7.2 \times 10^{-9}) \\ &= -(0.86) - (-9.00) \text{ \{Use log tables or your calculator to find the log of 7.2.\} } \\ &= 9.00 - 0.86 \\ &= 8.14\end{aligned}$$

19.5

You Try It

19.5

2. What is the pOH of a solution if the $[\text{OH}^-] = 3.5 \times 10^{-2} M$?

Your Solution

Example C

19.5

What is the pOH of a solution that has a pH of 3.4?

Solution

$$\begin{aligned}\text{pH} + \text{pOH} &= 14.0 \\ \text{pOH} &= 14.0 - \text{pH} \\ &= 14.0 - 3.4 \\ \text{pOH} &= 11.6\end{aligned}$$

You Try It

19.5

3. A solution has a pOH of 12.4. What is the pH of this solution?

Your Solution

Problems For You To Try

19.4, 19.5

4. Classify each solution as acidic, basic, or neutral

- $[\text{H}^+] = 2.5 \times 10^{-9} M$
- $\text{pOH} = 12.0$
- $[\text{OH}^-] = 9.8 \times 10^{-11} M$
- $[\text{H}^+] = 1 \times 10^{-7} M$
- $\text{pH} = 0.8$

19.4, 19.5

5. Calculate the pH of each solution.

- $[\text{H}^+] = 1 \times 10^{-5} M$
- $[\text{H}^+] = 4.4 \times 10^{-11} M$
- $[\text{OH}^-] = 2.2 \times 10^{-7} M$
- $\text{pOH} = 1.4$

19.4

6. Classify the solutions in Problem 5 as acidic or basic.

7. Why is there a minus sign in the definition of pH?

19.4, 19.5